

Exam for WSSA'03 Course on *Static Analysis*

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Answer 3 of the following 4 questions.

Note: In the questions that follow, I reference slides from the lectures, where I use numberings from the PS-files posted on my web page. Those numbers might not match exactly the ones in your notes, so please consult my web site if you are uncertain of a reference.

Question 1. Introduction to abstraction and static analysis

From Lecture 1, Slide 17 (“A Starting Point: Trace-Based Operational Semantics”) shows the trace-based operational semantics for a while-loop program.

Here is a syntax for the language in which the program was written:

```
P : ProgramPoint
C : Command
E : Expression
F : BasicExpression
x : Variable
N : Numeral

C ::= P: x := E | P: while E do C | C1 ; C2

E ::= F1 + F2 | F1 < F2
F ::= N | x
N ::= 0 | 1 | 2 | ...

P ::= p0 | p1 | p2 | ...
x ::= a | b | c | ...
```

Write an algorithm that translates a program written in the above language into a set of state transition rules that compute the program’s “concrete” execution semantics on integers.

Next, write an algorithm that translates a program written in the above language into a set of state transition rules that compute the program’s abstract semantics on the abstract data values, $\{even, odd\}$. (See Slide 18: “We can abstractly interpret, say, for polarity”).

Finally, write a proof that, for every program, the translated rules that compute the abstract values, $\{even, odd\}$, of variables are sound with respect to the rules that compute the concrete semantics. (Hint: Read Slides 20 and 21: “The underlying abstract interpretation semantics.”)

Question 2. Foundations of Abstract Interpretation

From Lecture 2, read Slides 14 and 15, “Closed binary relations.” Use the definition of γ on Slide 14 to prove the Proposition stated on Slide 15.

Question 3. Mechanics of Static Analysis

Slide 16 of Lecture 3 defines *forwards-necessarily reaching definitions analysis*.

Rewrite the definitions of $inReach(p_i)$ and $f_i^\#$ on that slide so that the analysis compute forwards-*possibly* reaching definitions analysis.

Use your definition to rewrite the abstract transfer functions for the program on Slide 9 and recompute the flow-analysis table for the program, which should look similar to the one on Slide 11.

Question 4. Static Analysis: Applications and Logics

In Lecture 4, Slide 17 (“Constructing an abstract logic”) shows how to generate a distributive complete lattice. Prove Items 1 and 2 on Slide 18.

Next, prove that the distributive lattice generated from $\{neg, zero, pos\}$, where

$$\begin{aligned} n &\models neg \text{ for all } n < 0 \\ n &\models pos \text{ for all } n > 0 \\ 0 &\models zero \end{aligned}$$

quotiented by the induced function, γ (that is, $A \equiv_\gamma B$ iff $\gamma(A) = \gamma(B)$), is exactly the **Signs** lattice, displayed at the bottom of Slide 18.